Inquiry Co-Operation Model: An Effort to Enhance Students’ Mathematical Literacy Proficiency

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ABSTRACT

The urgency and proficiency of students’ mathematical literacy in Bandung that have not been optimal are the basis of this study. The aim of this study is to explain the enhancement of students’ mathematical literacy proficiency due to the implementation of the inquiry co-operation model (experimental class) and conventional learning (control class) in terms of basic mathematical proficiency. This study is a quasi-experimental study with a non-equivalent control group design, and the research subjects were seventy students of class VIII of Bandung that were selected through a purposive sampling technique. The research data was obtained through mathematical literacy tests of material in a polyhedron. The results of the data analysis showed that: (1) the enhancement in mathematical literacy proficiency of the experimental students class was better than the control students class in terms of the basic mathematical proficiency (high and medium); (2) there is no significant difference in the increase of mathematical literacy proficiency in experimental students class in terms of the basic mathematical proficiency. It can be concluded that inquiry co-operation model espouses the enhancement of students’ mathematical literacy proficiency.

Keyword:
Basic Mathematical Proficiency; Inquiry Co-Operation Model; Mathematical Literacy; Mathematics Education.

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A. INTRODUCTION

One of the international standard assessments used as benchmarks to determine the quality of mathematical proficiency in Indonesia is the Program for International Student Assessment (PISA). The PISA study was conducted by OECD countries (Organization of Economic Corporation Development) and the UNESCO (United Nations Educational Scientific and Cultural Organization) Institute for Statistics (OECD, 2015). The mathematical proficiency measured by PISA is mathematical literacy. Mathematical literacy is the proficiency to formulate, apply, and interpret mathematics in various contexts. There are six levels of mathematical literacy proficiency in the PISA framework (OECD, 2016b). Level one is the proficiency to complete routine procedures, level two is the proficiency to apply basic algorithms, level three is the proficiency to implement problem-solving strategies, level four is the proficiency to combine different representations, level five reflects the results of work, and level six is the proficiency to develop strategies and new approaches in dealing with problems (OECD, 2015).
The importance of having mathematical literacy skills is also implied in the goals of mathematics education which are stated by the national council of mathematics teachers (NCTM, 2000). The importance of having mathematical literacy skills is in contrast with the results of the PISA study taken by Indonesian students. Based on the results of the PISA study in 2012, 2015, 2018 it can be concluded that the mathematical literacy proficiency of Indonesian students needs to be improved (OECD, 2014, 2016b, 2019). It turned out that the results of the PISA study were in line with the results of a preliminary study conducted by the author at one of the junior high schools in Bandung. The results of the preliminary study revealed that junior high school students in Bandung were still experiencing various difficulties in working on mathematical literacy problems. The questions used in the preliminary study are a matter of mathematical literacy created by PISA in 2012. Following in Figure 1 performed representations of student answers when answering mathematical literacy questions.

Refer to Figure 1, it appears that students answer these questions by calculating the beam volume. This means students have understood that the cubes will form the building blocks. However, students still experience obstacles in making block image representation. These results indicate that students are still experiencing difficulties with the content of the mathematical literacy process, which is to formulate mathematical problems with a description of the process of sketching to build a flat side space. In addition, students also have obstacles in reflecting the meaning of the questions given. In other words, students do not understand the purpose of the problem, so the students' answers do not match expectations.

Same as the results of the preliminary study, the study of Wulandari (2015) found that junior high school students in Bandung were still experiencing various problems in solving mathematical literacy problems. The constraints faced by students were not being able to identify data on the problem, reflect the meaning of the statement given, make conclusions from two unrelated facts, and interpret three related dimensional objects.
One solution that can be done to improve mathematical literacy is through learning mathematics in schools. Good mathematics learning has some criteria. Those are the relationship between the taught material and real-life, the enjoyable and interesting learning atmosphere, the encouragement of student participation, and the improvement of students’ thinking habits (Yang, 2012, p. 83). Furthermore, teaching mathematical literacy requires mathematical value, mathematical meaning, mathematics teaching practices, teacher insight and competences (Bolstad, 2019, p. 99). One learning method that meets these criteria is the Inquiry Co-operation Model (ICM). ICM learning is a combination of guided inquiry learning and free inquiry (namely modified free inquiry learning). Modified free inquiry learning can enhance students’ critical thinking and mastery concepts (Rahmi et al., 2020, p. 104). ICM learning is a learning model that emphasizes student activity in the process of inquiry, the discovery of a mathematical concept and solving problems related to daily life (AlrØ & Skovsmose, 2004). Several studies such as Effendi (2012), Purwatiningshih (2014), and Hasibuan & Irwan (2014) found that guided inquiry learning was better than conventional learning in enhancing a variety of mathematical proficiency.

This study not only focuses on learning that is carried out but also pays attention to aspects of students' Basic Mathematical Proficiency (BMP) because it is related to the effectiveness of learning implementation. BMP students have a role to learn new mathematical material that will be studied as Bruner's connectivity theorem, that in mathematics between one concept with another concept there is a close relationship, not only in terms of content but also in terms of formulas that are studied (Takaya, 2015). The purpose of paying attention to the BMP aspect is to find out whether the improvement in students’ mathematical literacy proficiency is evenly distributed in all BMP categories (high, medium, and low) or only certain BMP categories. If the improvement of mathematical literacy proficiency is evenly distributed in all BMP categories (high, medium, and low), then this study can be generalized that the application of ICM learning in mathematics learning is appropriate for all levels of proficiency.

### B. METHODS

This study aims to examine the effect of ICM learning on mathematical literacy proficiency. In its application, the sample is not randomly selected and the variables in this study cannot be controlled entirely, so this study is quasi-experimental. The research design used was a non-equivalent control group design modified from Creswell (2014, p. 285) as below:

![Experimental Class: O X O, Control Class: O O O](image)

Annotation $O$ is measurement of pre response and post response to the dependent variable, $X$ is treatment of inquiry co-operation model learning.

The subjects in this study were students of class VIII at one of the junior high schools in Bandung. Thirty five students of class VIII E as an experimental class (ICM study) and thirty five students of class VIII F as a control class (conventional learning). The instrument used was a mathematical literacy proficiency test on the material in polyhedron with indicators (1) formulating mathematical problems; (2) applying concepts, facts, procedures, and mathematical reasoning; (3) interpreting, using and evaluating mathematical results (OECD). Mathematical literacy proficiency in this study is reviewed from the Basic Mathematical Proficiency (BMP) students. BMP is grouped into three groups, (1) high BMP, (2) medium BMP, and (3) low BMP, with the following criteria (Lestari & Yudhanegara, 2017, p. 233).
According to mean ($\bar{x}$) and standard deviation ($s$) of the first semester score, students of experimental class and students of control class are grouped into three BMP groups (see Table 1). While, the magnitude of the enhancement in students’ mathematical literacy proficiency on experimental class and control class is calculated using the normalized gain (normalized gain) developed by Meltzer (2002) as follows:

$$n\text{-gain} = \frac{\text{post test score} - \text{pre test score}}{\text{ideal score} - \text{pre test score}}$$

The results of the $n$-gain calculation are then interpreted using the classification from Hake (1999) which can be seen in the following table.

<table>
<thead>
<tr>
<th>$n$-gain ($g$)</th>
<th>Category</th>
</tr>
</thead>
<tbody>
<tr>
<td>$g &lt; 0.3$</td>
<td>Low</td>
</tr>
<tr>
<td>$0.3 \leq g &lt; 0.7$</td>
<td>Medium</td>
</tr>
<tr>
<td>$g \geq 0.70$</td>
<td>High</td>
</tr>
</tbody>
</table>

C. RESULT AND DISCUSSION

The post-test results were processed to determine the percentage of final achievement of mathematical literacy proficiency. Each level percentage of students’ mathematical literacy proficiency can be seen in Figure 4. Referring to Figure 4, the percentage of students achieving mathematical literacy proficiency for each item who gets ICM learning was higher than students who get conventional learning. The highest percentage of students answering the questions correctly at level 1 questions was 93.33% for the experimental class and 83.80% for the control class. Meanwhile, the smallest percentage of students answering questions correctly at level 6 questions was 19.71% for the experimental class and 15.14% for the control class.
The results of the achievement at level 6 questions (see Figure 4) was in line with the PISA study which states that the proficiency of Indonesian students in answering questions at level 6 is still low (OECD, 2016c). The entire content of the process on mathematical literacy skills is contained in level 6 questions so that it made a complexity at level 6. The content of the process is to formulate problems mathematically; apply concepts, facts, procedures, and mathematical reasoning; and interpret, use, and evaluate mathematical results.

The pre-test, post-test, and n-gain scores of mathematical literacy proficiency of students who obtained ICM learning and who obtained conventional learning were processed in descriptive and inferential statistics. Descriptive statistical calculations include determining the maximum score, minimum score, average score, and standard deviation of the score. A description of the mathematical literacy proficiency of students who obtained learning of ICM and conventional is presented in Table 3.

<table>
<thead>
<tr>
<th>BMP Category</th>
<th>ICM</th>
<th>CL</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Pre-Test</td>
<td>Post-Test</td>
</tr>
<tr>
<td>High</td>
<td>7</td>
<td>22</td>
</tr>
<tr>
<td></td>
<td>(%)</td>
<td></td>
</tr>
<tr>
<td></td>
<td>20</td>
<td>62.86</td>
</tr>
<tr>
<td></td>
<td>1.92</td>
<td>3.59</td>
</tr>
<tr>
<td>Medium</td>
<td>5.65</td>
<td>19.50</td>
</tr>
<tr>
<td></td>
<td>(%)</td>
<td></td>
</tr>
<tr>
<td></td>
<td>16.57</td>
<td>55.71</td>
</tr>
<tr>
<td></td>
<td>1.56</td>
<td>4.21</td>
</tr>
<tr>
<td>Low</td>
<td>5.43</td>
<td>19.29</td>
</tr>
<tr>
<td></td>
<td>(%)</td>
<td></td>
</tr>
<tr>
<td></td>
<td>15.51</td>
<td>55.10</td>
</tr>
<tr>
<td></td>
<td>0.53</td>
<td>4.79</td>
</tr>
</tbody>
</table>

Ideal score = 35 and ideal n-gain = 1

Referring to Table 3, the basic mathematical literacy proficiency of high and medium BMP students who get conventional learning is higher than students who receive ICM learning. However, for the low BMP category, the initial literacy proficiency of students who get ICM learning is higher than students who get conventional learning. While the final achievement of the mathematical literacy proficiency of the experimental class students based on the high, medium and low BMP categories were respectively 62.86%, 55.71%, and 55.1% of the ideal score. However, the percentage of post-test achievement of control class students in the high, medium, and low BMP categories was respectively 47.76%, 47.46%, and 45.14% of the ideal score. Post-test scores of experimental class students when viewed from BMP are more diverse than control class students. Pre-test and post-test scores were processed to obtain n-gain values. The n-gain value serves to measure the increase of students' mathematical literacy proficiency. When viewed from the BMP category, the average percentage of n-gain categories of the high, medium, and low BMP who obtained ICM learning was higher than students who obtained normal learning.

The n-gain data test of mathematical literacy proficiency based on the BMP category is used to test the hypothesis that students who get ICM learning is better than students who obtain conventional learning in increasing mathematical literacy proficiency when viewed from the initial mathematical proficiency (high, medium, low). Previously, the prerequisite tests, normality and homogeneity tests, were carried out first. The normality test used is the Shapiro Wilk test at the significance level α = 0.05. Shapiro Wilk's test results showed that the n-gain of each BMP category in both classes was normally distributed. While for the homogeneity test, a Levene test with significance level α = 0.05 was used. Levene test results revealed that the high and low n-gain BMP had homogeneous variance. These results indicate
an increase in the mathematical literacy proficiency of high and low BMP students to spread evenly. Conversely, n-gain BMP is having an inhomogeneous variance.

After concluding that the n-gain mathematical literacy proficiency of high BMP is normal and homogeneous distribution, then the average difference test with a t-test is performed. While the n-gain mathematical literacy proficiency of medium and low BMP is normally distributed but not homogeneous, then it is continued with a t-test with a significance level \( \alpha = 0.05 \) as shown in Table 4.

<table>
<thead>
<tr>
<th>BMP</th>
<th>( T )</th>
<th>( t' )</th>
<th>( df )</th>
<th>Sig. (1-tailed)</th>
<th>Decision</th>
<th>Annotation</th>
</tr>
</thead>
<tbody>
<tr>
<td>High</td>
<td>3.634</td>
<td>-</td>
<td>13</td>
<td>0.0015</td>
<td>( H_0 ) Rejected</td>
<td>Better</td>
</tr>
<tr>
<td>Medium</td>
<td>-</td>
<td>3.184</td>
<td>36</td>
<td>0.002</td>
<td>( H_0 ) Rejected</td>
<td>Better</td>
</tr>
<tr>
<td>Low</td>
<td>-</td>
<td>1.712</td>
<td>13</td>
<td>0.066</td>
<td>( H_0 ) Accepted</td>
<td>Not Better</td>
</tr>
</tbody>
</table>

Referring to Table 4, it can be concluded that students who obtain ICM learning is significantly better than students who obtain normal learning in the high and medium BMP category students who have an average n-gain mathematical literacy proficiency. On the other hand, low BMP students who get ICM learning are no better than low BMP students who get conventional learning.

Hypothesis testing is then carried out to determine differences in the increase of mathematical literacy proficiency of students in each BMP category who obtained ICM learning. Previously, a homogeneity test was carried out through the Levene test with the significance level \( \alpha = 0.05 \). Levene test results show that overall n-gain has a homogeneous variance. So that the test continued with One Way ANOVA test at the level of significance \( \alpha = 0.05 \) as shown in Table 5.

<table>
<thead>
<tr>
<th>( F )</th>
<th>Sig. (2-tailed)</th>
<th>Decision</th>
<th>Annotation</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.687</td>
<td>0.510</td>
<td>( H_0 ) Accepted</td>
<td>There is no difference</td>
</tr>
</tbody>
</table>

Table 5 shows that there is no significant difference in increasing the mathematical literacy proficiency of students who obtain ICM learning when viewed from the BMP category (high, medium, and low).

The n-gain test results show that increasing the mathematical literacy proficiency of high and medium BMP students who obtain ICM learning in the moderate category is significantly better than high and medium BMP students who obtain normal learning in the medium category. On the other hand, the increase on mathematical literacy skills of low BMP students who received medium category ICM learning was not significantly better than those of low category BMP students who obtained conventional learning. The factor that caused this finding to occur was the existence of advocating stages in ICM learning. The advocating stage raises the scaffolding process between high BMP students, medium BMP students, and low BMP students.

As expressed by Vygotsky that with the scaffolding process between students, it will cause students to reach the upper limit of ZPD (Zone of Proximal Development) (Fani & Ghaemi, 2011; Muhonen et al., 2016; Zhang & Whitebread, 2017). The scaffolding process helps students of the medium and low BMP categories because all students can exchange ideas during the process of solving problems, and gain learning experiences from students of the high BMP category. However, low BMP category students did not maximize the scaffolding process in this study. Some problems usually arise in students with low proficiency in learning mathematics. They are more likely to be slow than moderate or high proficiency students.
Although, they are given the opportunity to share and ask questions in discussion activities, but their opportunity is not often utilized as well as possible.

A more in-depth review of the differences in the improvement of mathematical literacy proficiency of BMP students (high, medium, and low) who obtained ICM learning revealed that there was no significant difference in the increase on mathematical literacy skills of students who obtained ICM learning when viewed from BMP (high, medium, and low). The results of this statistical test indicate that the increased literacy proficiency of high, medium and low proficiency students is statistically similar. These results are in line with the findings of Pujiastuti, et al (2014). This finding arises as a result of ICM learning in the process of linking prior mathematical proficiency when learning new material, especially at the stages of locating, identifying, advocating, reformulating, and challenging. Thus, all students become accustomed to recalling previous mathematics material which is useful for learning new material.

In addition to statistical analysis as explained. Next is an analysis of increasing students' mathematical literacy proficiency through the results of the pre-test and post-test. Mathematical literacy problems level 1 to level 3 were constructed by (Malasari et al., 2017). While the mathematical literacy problems level 4 to level 6 were constructed by researchers. The following is a mathematical literacy problem at level 3 (see Figure 5).

![Mathematical literacy problem at level 3](image)

**Figure 5.** Mathematical literacy problem at level 3

Presented the results of the pre-test and post-test at level 3 of mathematical literacy problem (see Figure 6 and Figure 7).

![The Result of Pre-test](image)

**Figure 6.** The Result of Pre-test

![The Result of Post-test](image)

**Figure 7.** The Result of Post-test
Referring to Figure 6, in the results of the pre-test, students write 120 pieces as the number of boxes to fill into the container based on\( V = p \times l \times t = 6 \times 5 \times 4 = 120 \). However, in the post-test Figure 7, an increase was seen in determining the number of boxes already in the box and determining the final result of the number of boxes needed to fill the container. An example of an increase at the time of the post-test was, students wrote if there were as many boxes already in the box 22 pieces, the number of boxes still needed to fill the container is 120 boxes - 22 boxes = 98 boxes. Based on the dimensions of the cognitive process of bloom revision taxonomy, level 3 questions are the dimensions of applying (C.3.). This is because level 3 questions require students' ability to implement volume formulas and surface area of flat side space (Pappas et al., 2013). The ability to apply turns out to be in harmony with higher levels of thinking according to Pappas et al (2013).

D. CONCLUSION AND SUGGESTIONS

Based on the results of the quantitative analysis and the discussion in the previous description, it can be concluded into two conclusions. First, increasing the mathematical literacy proficiency of students who get ICM learning is significantly better than students who get conventional learning when viewed from the high and medium BMP categories. This finding apparently did not occur in students with a low BMP category. Students who get ICM learning are not significantly better than students who get conventional learning in the category when reviewed by BMP in the low category. The cause of this finding occurs because high and medium BMP students can maximize the stages of advocating on ICM learning so that the process of exchanging ideas, asking questions, and supporting each other in solving mathematical literacy problems can run optimally. Conversely, low BMP students apparently cannot maximize the advocating stage. Second, there is no significant difference in the increase on mathematical literacy skills of students who get ICM learning when viewed from the high, medium, and low BMP categories. The second finding arises because the stages of locating, identifying, advocating, reformulating, and challenging in ICM learning supports the process of attributing students’ mathematical proficiency when learning new material. Although the statistical test results showed no difference, the average n-gain value actually showed an increase on mathematical literacy proficiency of students in the high BMP category which is higher than students in the moderate and low BMP categories.

The next findings are that the percentage of student achievement in solving level 6 of mathematical literacy questions is still low, it would be better to maximize the process of implementing the challenging stages of ICM learning through giving mathematical literacy problems which are more challenging and solved in groups. In addition, it is better to maximize students’ proficiency to solve mathematical literacy problems from questions level 1 to level 5 firstly because level 6 are the highest level in mathematical literacy proficiency.

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REFERENCES


